

# The Dual-Detector Argument Against the Modal Theory

DAN MARSHALL

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# 1 The Dual-Detector Argument Against 2 the Modal Theory

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3 The modal theory holds that facts (properties) are identical iff they are  
4 necessarily equivalent (coextensive). One of the most prominent argu-  
5 ments against the modal theory is Elliot Sober's dual-detector argument.  
6 According to this argument, the fact that some particular thing is a trian-  
7 gle is distinct from the necessarily equivalent fact that it is a trilateral,  
8 since it is only the former fact that causes an output of a certain machine.  
9 I argue that the dual-detector argument fails, in part because whatever  
10 initial plausibility it has relies on the failure to take into consideration a  
11 needed relativisation to times and the failure to distinguish between two  
12 facts collectively causing a fact and their conjunction singly causing it. I  
13 also argue that variants of the argument are equally unsuccessful.

14 One of the most popular and well known accounts of the identity-conditions  
15 of facts and properties is the modal theory.<sup>1</sup> According to this theory: i) two  
16 facts are identical iff they are necessarily equivalent to each other; and ii)  
17 two properties are identical iff they are necessarily coextensive to each other.  
18 That is, the modal theory holds that: i) the fact that  $\phi$  = the fact that  $\psi$  iff,  
19 necessarily, ( $\phi$  iff  $\psi$ ); and ii) the property of being  $F$  = the property of being  
20  $G$  iff, necessarily, for any  $x$ , ( $x$  is  $F$  iff  $x$  is  $G$ ).<sup>2</sup> This theory is prima facie  
21 attractive, since it is simple to formulate and provides an account of the

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1 A fact, as I will understand it here, is an obtaining state of affairs, where: i) a state of affairs is either a way things are or a way things aren't, and ii) a state of affairs obtains iff it is a way things are. A fact on this understanding is therefore just as way things are. Proponents of the modal theory include Stalnaker (1984), Lewis (1986a), and Jackson (1998).

2 For simplicity, I will assume necessitism, according to which, necessarily, for any  $x$ , necessarily, for some  $y$ ,  $x = y$ . (Without this assumption, 'necessarily, for any  $x$ ' needs to be replaced with 'necessarily, for any  $x$ , necessarily' in the above characterisation of the modal theory.) I will also assume an abundant theory of facts and properties according to which (except for restrictions needed to avoid paradox), all true sentences express facts, and all predicates that can be used to form true or false sentences express properties.

identity-conditions of facts and properties in terms of (at least relatively) well understood notions. Everything else being equal, the theory is also more parsimonious than rival theories that reject it, since, everything else being equal, there are less facts if the modal theory holds than if it fails to hold and there are distinct facts that are necessarily equivalent to each other.

A prominent argument against the modal theory is the dual-detector argument originally due to Elliot Sober.<sup>3</sup> Briefly, according to this argument, there could be a machine that, as a result of containing detectors measuring different aspects of an input, is causally sensitive to one fact without being causally sensitive to another necessarily equivalent fact. Since, by Leibniz's law, it follows from this that, contra the modal theory, there are distinct facts that are necessarily equivalent to each other, the argument concludes that the modal theory is false. Despite this argument's prominence, discussions of the argument by both its proponents and opponents have been brief and cursory. This paper will provide a more sustained evaluation of the dual-detector argument and will argue that such an evaluation shows that the argument is unsuccessful.<sup>4</sup>

I will proceed as follows. In section 1, I will formulate the dual-detector argument before then arguing in section 2 that it is unsuccessful. In section 3, I will then consider two variants of the argument and I will argue that these variants, and more generally that all variants, are also unsuccessful.

Before proceeding to section 1, it will be useful to briefly discuss another common argument against the modal theory—the constituency argument—in order to set it aside (see, for example, Audi 2016). Suppose (1) and (2) are true, where '*W*' refers to some particular wire.

- (1) *W* is a closed straight-sided figure that has three *angles*.
- (2) *W* is a closed straight-sided figure that has three *sides*.

According to the constituency argument, since the fact expressed by (1) has angularity as a constituent while the fact expressed by (2) doesn't have this property as a constituent, the facts expressed by (1) and (2) are not identical

<sup>3</sup> See Sober (1982). A similar argument is also given by Enç (1982). A recent proponent of the dual-detector argument, for example, is Audi (2016). Other philosophers who are sympathetic to the argument include Miller (1995, 859) and Molnar (2003, 66). Opponents of the argument include Jackson (1998, 125–126) and Armstrong (1997, 145–146).

<sup>4</sup> Two other arguments against the modal theory that appeal to causation have been given by Achinstein (1974) and Perry (1989). Sober (1982, 84–85) gives what I take to be a convincing response to Achinstein's argument. For a response to Perry's argument, see Marshall (2021).

52 to each other. Since the modal theory entails that the facts expressed by (1)  
 53 and (2) are identical to each other (since they are necessarily equivalent to  
 54 each other), the constituency argument concludes from this that the modal  
 55 theory is false.

56 The constituency argument arguably begs the question against the modal  
 57 theory by in effect assuming the rival structured theory of facts. According to  
 58 this rival theory, facts are structured in the same kind of way that sentences  
 59 are structured. In particular, according to the structured theory, facts are built  
 60 up out of objects, properties, relations, operators and quantifiers in the same  
 61 way that sentences are built up out of names, predicates, operator expressions  
 62 and quantifier expressions.<sup>5</sup> If the structured theory holds so that the facts  
 63 expressed by (1) and (2) are built up out of objects, properties, relations,  
 64 operators and quantifiers in the same kind of way that sentences are built up  
 65 out of names, predicates and other expressions, then it is plausible that the  
 66 fact expressed by (1) has angularity as a constituent while the fact expressed  
 67 by (2) doesn't have this constituent. This is much less plausible, however, if  
 68 the structured theory is false and facts aren't structured like sentences. For  
 69 example, if facts are instead structured like visual experiences or pictures, then,  
 70 since it is prima facie plausible to associate (1) and (2) with the same (type) of  
 71 visual experience or picture, it is prima facie plausible that (1) and (2) express  
 72 the same fact and hence prima facie plausible that the facts expressed by (1)  
 73 and (2) don't differ in what constituents they have. (This is because it is at  
 74 least prima facie plausible that any picture that represents  $W$  as being a closed  
 75 straight-sided figure that has three *angles* also represents  $W$  as being a closed  
 76 straight-sided figure that has three *sides*, and vice versa.) Since the argument  
 77 from constituency provides no reason to think that facts are structured in  
 78 the way that the structured theory holds that they are structured, rather than  
 79 some other way, the argument therefore fails to provide a good reason to think  
 80 that (1) and (2) express distinct facts and hence fails to provide a good reason  
 81 to reject the modal theory.

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5 The structured theory can be formulated more precisely as a thesis endorsing schemas such as (PS) and (OS) (see, for example, [Dorr 2016, 58–59](#)).

PS. For any  $x$  and  $y$ , if the fact that  $x$  is  $F$  = the fact that  $y$  is  $G$ , then: i)  $x = y$ , and ii) the property of being  $F$  = the property of being  $G$ .

OS. If the fact that  $\pi_1(\phi_1)$  = the fact that  $\pi_2(\phi_2)$ , then: i) the operator of  $\pi_1$  = the operator of  $\pi_2$ , and ii) the state of affairs of it being that  $\phi_1$  = the state of affairs of it being that  $\phi_2$ .

82 It is important to appreciate that the structured theory is neither self-evident  
 83 nor prima facie highly plausible, and hence it cannot simply be assumed to  
 84 hold in the above argument from constituency without begging the question  
 85 against the modal theory. Three brief reasons for this are the following: First,  
 86 prior to investigation and argument, the claim that facts are structured like  
 87 sentences is no more plausible than the claim that facts have some other type  
 88 of structure, such as that of visual experiences or pictures. Second, while (1)  
 89 and (2) arguably differ in their cognitive significance, since a linguistically  
 90 competent person arguably might endorse one of them while rejecting the  
 91 other, such a difference in cognitive significance is widely thought to be able to  
 92 be explained by a difference in what mode of presentation the facts expressed  
 93 by (1) and (2) have when expressed by these sentences, where this explanation  
 94 does not require that the facts expressed by these sentences are non-identical  
 95 (see, for example, Braun 1998; McKay and Nelson 2010). Third, the structured  
 96 theory conflicts with claims that are widely thought to be at least as prima  
 97 facie plausible as the structured theory itself, such as the claim made by (3).

98 (3) '*W* is self-identical' expresses the same fact as '*W* is identical to *W*'.  
 99 (3) conflicts with the structured theory, since, if the structured theory is  
 100 true, the fact expressed by '*W* is self-identical' has the property of being self-  
 101 identical as a constituent while the fact expressed by '*W* is identical to *W*'  
 102 lacks this constituent and instead has the property of being identical to *W* as a  
 103 constituent.<sup>6</sup> Due to the above difficulty with the constituency argument, and  
 104 since we cannot simply assume the structured theory in arguing against the  
 105 modal theory, I will assume in the following that the constituency argument  
 106 against the modal theory fails.

## 107 **1 The Dual-Detector Argument**

108 The dual-detector argument is not meant to rely on the cogency of the consti-  
 109 tuency argument discussed above, nor is it meant to rely on the truth of the  
 110 structured theory of facts. Instead, the dual-detector argument is meant  
 111 to provide a separate reason for rejecting the modal theory. The argument

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6 A further possible consideration against the structured theory is that, unlike the modal theory, it gives rise to the Myhill-Russell paradox. See, for example, Dorr (2016) and Goodman (2017). For attempted solutions to the Myhill-Russell paradox that are compatible with the structured theory, see, for example, Walsh (2016), Kment (2022) and Yu (2017). See Dorr (2016) and Bjerring and Schwarz (2017) for further arguments against the structured theory.

112 involves a machine *M* that contains two detectors: a closed straight-sided  
113 figure detector and a three-angle detector. These detectors are linked in a  
114 series in *M*, so that, if a wire (or several wires) are inputted into *M*, they are  
115 first inputted into the closed straight-sided figure detector and then, if they are  
116 outputted by this first detector, they are inputted into the three-angle detector.  
117 If the wire (or wires) are then outputted by the three-angle detector, they are  
118 then outputted by *M*. Indeed, I will assume in the following that what it is for  
119 something (or some things) to be outputted by *M* is just for it (or them) to be  
120 outputted by this second detector.

121 The closed straight-sided figure detector in *M* works so that “when given a  
122 piece of wire as input, it will output the piece of wire if and only if the wire is  
123 a closed [(plane)] figure and all sides of the figure are straight” (Sober 1982,  
124 185). More explicitly, let us say that: i) when given a piece of wire as input  
125 that is a closed figure all of whose sides are straight, the closed straight-sided  
126 figure detector outputs the wire, and it does this *because* the wire is a closed  
127 figure all of whose sides are straight; whereas, ii) when given a piece of wire  
128 (or several pieces of wire) as input that is not a single closed figure all of  
129 whose sides are straight, the closed-straight-sided figure detector does not  
130 output it (or them). The three-angle detector, on the other hand, works so  
131 that “when given any number of straight pieces of wire, it outputs them if  
132 and only if they have three angles” (Sober 1982, 185). More explicitly: i) when  
133 given one or more pieces of wire with straight sides that collectively have  
134 three angles, the three-angle detector outputs them and it does this *because*  
135 the wire (or wires) collectively have three angles; whereas, ii) when given  
136 one or more pieces of wire with straight sides that don’t collectively have  
137 three angles, the three-angle detector does not output them. The three-angle  
138 detector is causally sensitive to whether the input has three angles, and not  
139 to whether it has three sides, since, when given a four-sided open figure, it  
140 will output the object (since it has three angles), and it will fail to do this if  
141 the four-sided figure is closed. In addition, when the three-angle detector is  
142 given three unconnected pieces of wire, each containing exactly one angle,  
143 the detector will output them, even though it is made up of six straight line  
144 segments.

145 Sober states the dual-detector argument as follows:

146 Now consider a particular object—a piece of wire—which is fed  
147 into the machine, passes through both [detectors], and is then  
148 outputted by the machine. What property of the object *caused* it

149 to be outputted? Given the mechanism at work here, I think that  
 150 the cause was the object's having the property of being a *closed*  
 151 *straight-sided figure having three angles* (i.e., its being a triangle),  
 152 and not its being a *closed straight-sided figure having three sides*  
 153 (i.e., its being a trilateral). If this is right, and if a difference in  
 154 causal efficacy is enough to insure a difference in property, it  
 155 follows that being a triangle is not the same property as being  
 156 a trilateral, even though "triangle" and "trilateral" are logically  
 157 (mathematically) equivalent. (Sober 1982, 185, author's emphasis)

158 Let [ $\phi$ ] abbreviate 'the fact that  $\phi$ ', and suppose that  $W$  is the piece of wire  
 159 that is fed into  $M$ . Let us also suppose that the above process of  $W$  being fed  
 160 into and then being sequentially outputted by the two detectors has occurred.  
 161 Then, according to Sober's dual-detector argument, (ANGLE) is true while  
 162 (SIDE) is false.

163 ANGLE. [ $W$  is a closed straight-sided figure that has three *angles*]  
 164 causes [ $M$  outputs  $W$ ].

165 SIDE. [ $W$  is a closed straight-sided figure that has three *sides*] causes  
 166 [ $M$  outputs  $W$ ].

167 The dual-detector argument then employs Leibniz's law to infer from this  
 168 that, since they differ in what they cause, [ $W$  is a closed straight-sided figure  
 169 having three *angles*] is not identical to the necessarily equivalent [ $W$  is a  
 170 closed straight-sided figure having three *sides*]. The argument then infers  
 171 from (4) and the non-identity of these facts that the property of being a closed  
 172 straight-sided figure that has three *angles* (or being triangular) is not identical  
 173 to the necessarily coextensive property of being a closed straight-sided figure  
 174 that has three *sides* (or being trilateral).

175 (4) For any  $x$ , IF  $x$  is  $F$ ,  $x$  is  $G$ , and the property of being  $F$  = the property  
 176 of being  $G$ , THEN [ $x$  is  $F$ ] = [ $x$  is  $G$ ].

177 Since these facts and properties are respectively necessarily equivalent to each  
 178 other and necessarily coextensive with each other (and hence are identical to

179 each other according to the modal theory), the dual-detector argument then  
 180 concludes from the above results that the modal theory is false.<sup>7</sup>

## 182 **Against the Dual-Detector Argument**

182 One initial problem with the dual-detector argument is that (ANGLE) is not  
 183 strictly speaking true, at least if we assume as we did above that the above  
 184 described process involving *W* and *M* has already occurred.

185 ANGLE. [*W* is a closed straight-sided figure that has three *angles*]  
 186 causes [*M* outputs *W*].

187 To see why this is the case, let us suppose that, after being fed into *M* and put  
 188 inside the closed straight-sided figure detector at  $t_1$ , *W* is outputted by the  
 189 closed straight-sided figure detector so that, at  $t_2$ , *W* is inside the three-angle  
 190 detector. Let us also suppose that *W* being inside the three-angle detector at  
 191  $t_2$  results in *W* being outputted by the three-angle detector at  $t_3$ , and hence  
 192 results in *W* being outputted by *M* at  $t_3$ . Finally, let us also suppose that the  
 193 times  $t_1$ ,  $t_2$  and  $t_3$  are all past times. Then the fact that *W* is a closed straight-  
 194 sided figure that has three angles (either simpliciter or at the present time)  
 195 does not cause *M* to do anything to *W*, since *W* is no longer interacting with  
 196 *M*.

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7 I am assuming that facts can cause other facts, where this claim is compatible with it also being the case that events can cause other events. If it is instead held that it is only events that can be causal relata, then 'fact' can be replaced with 'event' in the above presentation of the dual-detector argument to get the conclusion that there are distinct necessarily equivalent events (where two events are necessarily equivalent iff, necessarily, they either both occur or they both fail to occur). This conclusion together with (A) entails that there are distinct necessarily equivalent properties which, given (MF), entails that there are distinct necessarily equivalent states of affairs.

A. If the property of being *F* = the property of being *G*, then, for any *x*, the event of *x* having *F* = the event of *x* having *G*.

MF. The property of being *F* = the property of being *G* iff, necessarily, for any *x*, the state of affairs of *x* being *F* = the state of affairs of *x* being *G*.

Taking facts to be obtaining states of affairs (as in footnote 1), it follows from this that there are distinct necessarily equivalent facts.



197 The above problem with the dual-detector argument shows that, as it is  
 198 most charitably understood, it is not (**ANGLE**) that is true according to the  
 199 argument, but is instead either (**ANGLE**<sub>*t*<sub>1</sub></sub>) or (**ANGLE**<sub>*t*<sub>2</sub></sub>).<sup>8</sup>

200 **ANGLE**<sub>*t*<sub>1</sub></sub>. [*At t*<sub>1</sub>, *W* is a closed straight-sided figure that has three  
 201 *angles*] causes [*M* outputs *W* at *t*<sub>3</sub>].

202 **ANGLE**<sub>*t*<sub>2</sub></sub>. [*At t*<sub>2</sub>, *W* is a closed straight-sided figure that has three  
 203 *angles*] causes [*M* outputs *W* at *t*<sub>3</sub>].

204 As a result of this need to relativise to either time *t*<sub>1</sub> or time *t*<sub>2</sub>, we therefore  
 205 have two versions of the dual-detector argument. The first version—the *t*<sub>1</sub>-  
 206 version—holds that (**ANGLE**<sub>*t*<sub>1</sub></sub>) is true and (**SIDE**<sub>*t*<sub>1</sub></sub>) is false, from which it  
 207 infers that, contra the modal theory, the necessarily equivalent facts [*at t*<sub>1</sub>, *W*  
 208 is a closed straight-sided figure that has three *angles*] and [*at t*<sub>1</sub>, *W* is a closed  
 209 straight-sided figure that has three *sides*] are non-identical.

210 **SIDE**<sub>*t*<sub>1</sub></sub>. [*At t*<sub>1</sub>, *W* is a closed straight-sided figure that has three *sides*]  
 211 causes [*M* outputs *W* at *t*<sub>3</sub>].

212 The second version of the dual-detector argument—the *t*<sub>2</sub>-version—holds  
 213 instead that (**ANGLE**<sub>*t*<sub>2</sub></sub>) is true and (**SIDE**<sub>*t*<sub>2</sub></sub>) is false, from which it infers that,  
 214 contra the modal theory, the necessarily equivalent facts [*at t*<sub>2</sub>, *W* is a closed  
 215 straight-sided figure that has three *angles*] and [*at t*<sub>2</sub>, *W* is a closed straight-  
 216 sided figure that has three *sides*] are non-identical.

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8 In response to the above problem with Sober's (1982) original formulation of the dual-detector argument, we might modify *M* so that its two detectors act on *W* at the same time rather than sequentially. Such a modified version of the argument faces the same difficulties as the *t*<sub>1</sub>-version of the argument discussed below. First, given this modification, while it is plausible that (**ANGLE**<sup>\*</sup>) is true and (**SIDE**<sup>\*</sup>) is false (when relativised uniformly to the relevant time), there is an exclusion argument that argues from the truth of (**ANGLE**<sup>\*</sup>) to the falsity of (**ANGLE**).

**ANGLE**<sup>\*</sup>. [*W* is a closed straight-sided figure] and [*W* has three *angles*] collectively cause [*M* outputs *W*].

**SIDE**<sup>\*</sup>. [*W* is a closed straight-sided figure] and [*W* has three *sides*] collectively cause [*M* outputs *W*].

Second, this modified version of the argument faces the problem that, even if this exclusion argument is rejected, it doesn't seem possible to justify both the truth of (**ANGLE**) and the falsity of (**SIDE**).

217 SIDE<sub>t<sub>2</sub></sub>. [At t<sub>2</sub>, W is a closed straight-sided figure that has three sides]  
 218 causes [M outputs W at t<sub>3</sub>].

219 As we will see, both these versions of the dual-detector argument have serious  
 220 problems.<sup>9</sup>

221 The t<sub>2</sub>-version of the dual-detector argument can be quickly seen to fail  
 222 as follows: It is [W has three angles at t<sub>2</sub>] that causes W to be outputted by  
 223 the three-angle detector at t<sub>3</sub>, rather than say [at t<sub>2</sub>, W has three angles and  
 224 is blue] that causes this fact (even supposing that W is blue at t<sub>2</sub>). This is  
 225 intuitively because [at t<sub>2</sub>, W has three angles and is blue] goes beyond what  
 226 is causally relevant to whether W is outputted by the three-angle detector at  
 227 t<sub>3</sub>. Similarly, it is [W has three angles at t<sub>2</sub>] that causes W to be outputted by  
 228 the three-angle detector at t<sub>3</sub> rather than [at t<sub>2</sub>, W is a closed straight-sided  
 229 figure that has three angles] that causes this fact. This is because the latter  
 230 fact also goes beyond what is causally relevant to whether W gets outputted  
 231 by the three-angle detector at t<sub>3</sub>. Since W getting outputted by the three-angle  
 232 detector just is what it is for M to be outputted by W, it follows that (ANGLE<sub>t<sub>2</sub></sub>)  
 233 is false.

234 ANGLE<sub>t<sub>2</sub></sub>. [At t<sub>2</sub>, W is a closed straight-sided figure that has three  
 235 angles] causes [M outputs W at t<sub>3</sub>].

236 Since the falsity of (ANGLE<sub>t<sub>2</sub></sub>) conflicts with the t<sub>2</sub>-version of the dual-detector  
 237 argument, this version of the argument fails.

238 I will now argue that the t<sub>1</sub>-version of dual-detector argument is also unsuccess-  
 239 ful and hence that both versions of the dual-detector argument fail. I will  
 240 do this by first giving an argument from causal exclusion that, contrary to the

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9 There is also a temporally mixed version of the dual-detector argument that holds that (ANGLE<sub>t<sub>1</sub>,t<sub>2</sub></sub>) is true and (SIDE<sub>t<sub>1</sub>,t<sub>2</sub></sub>) is false.

ANGLE<sub>t<sub>1</sub>,t<sub>2</sub></sub>. [W is a closed straight-sided figure at t<sub>1</sub> that has three angles at t<sub>2</sub>] causes [M outputs W at t<sub>3</sub>].

SIDE<sub>t<sub>1</sub>,t<sub>2</sub></sub>. [W is a closed straight-sided figure at t<sub>1</sub> that has three sides at t<sub>2</sub>] causes [M outputs W at t<sub>3</sub>].

This version of the argument at best only shows that [W is a closed straight-sided figure at t<sub>1</sub> that has three angles at t<sub>2</sub>] is not identical to [W is a closed straight-sided figure at t<sub>1</sub> that has three sides at t<sub>2</sub>], which does not conflict with the modal theory since these facts are not necessarily equivalent to each other.

241 dual-detector argument, ( $\text{ANGLE}_{t_1}$ ) is false. I will then argue that, even if this  
 242 causal exclusion argument is rejected, it is not possible to justify both the truth  
 243 of ( $\text{ANGLE}_{t_1}$ ) and the falsity of ( $\text{SIDE}_{t_1}$ ), the justification of both of which is  
 244 required for the  $t_1$ -version of the argument to be successful. (Or at least, I will  
 245 argue that one cannot justify the truth of ( $\text{ANGLE}_{t_1}$ ) and the falsity of ( $\text{SIDE}_{t_1}$ )  
 246 without appealing to some other argument against the modal theory that, if  
 247 successful, would refute the modal theory by itself and hence would render  
 248 the dual-detector argument superfluous.)

249 To set up the needed background for the argument from causal exclusion  
 250 against ( $\text{ANGLE}_{t_1}$ ), note that, in the case of  $M$  processing  $W$ , [ $W$  is a closed  
 251 straight-sided figure at  $t_1$ ] causes  $W$  to be outputted by the closed straight-  
 252 sided figure detector, and so causes  $W$  to be in the three-angle detector at  $t_2$ .  
 253 Hence we have (5)

254 (5) [ $W$  is a closed straight-sided figure at  $t_1$ ] causes [ $W$  is in the three-angle  
 255 detector at  $t_2$ ].

256 Since [ $W$  is in the three-angle detector at  $t_2$ ] and [ $W$  has three angles at  $t_2$ ]  
 257 collectively cause  $W$  to be outputted by the three-angle detector at  $t_3$ , which  
 258 is what it is to be outputted by  $M$  at  $t_3$ , we also have (6).

259 (6) [ $W$  is in the three-angle detector at  $t_2$ ] and [ $W$  has three angles at  $t_2$ ]  
 260 collectively cause [ $M$  outputs  $W$  at  $t_3$ ].

261 Since plausibly one of the causes of  $W$  having three angles at  $t_2$  is that it had  
 262 three angles at previous times before  $t_2$ , (7) plausibly also holds.

263 (7) [ $W$  has three angles at  $t_1$ ] causes [ $W$  has three angles at  $t_2$ ].

264 Assuming, as is plausible, that the causal transitivity principle (T) holds in  
 265 this causal situation, (5–7) then entail ( $\text{ANGLE}_{t_1}^*$ ).<sup>10</sup>

266 T. IF the members of  $\Phi_1$  collectively cause  $r_1$ , the members of  $\Phi_2$   
 267 collectively cause  $r_2 \dots$  and  $r_1, r_2 \dots$  collectively cause  $r$ ; THEN the  
 268 members of  $\Phi_1 \cup \Phi_2 \cup \dots$  collectively cause  $r$ .

10 While causation is plausibly transitive in many typical cases, such as in the case above, many philosophers hold that causation is not unrestrictedly transitive. For alleged counterexamples to transitivity, see, for example, Kvart (1991) and McDermott (1995). For a defense of transitivity unrestrictedly holding, see Hall (2000).

269 ANGLE<sub>t<sub>1</sub></sub>\*. [*W* is a closed straight-sided figure at *t*<sub>1</sub>] and [*W* has three  
270 angles at *t*<sub>1</sub>] collectively cause [*M* outputs *W* at *t*<sub>3</sub>].

271 With the above background in place, it might seem like it should now be  
272 easy to derive (ANGLE<sub>t<sub>1</sub></sub>) from (ANGLE<sub>t<sub>1</sub></sub>\*), and hence establish that (ANGLE<sub>t<sub>1</sub></sub>)  
273 holds.

274 ANGLE<sub>t<sub>1</sub></sub>. [At *t*<sub>1</sub>, *W* is a closed straight-sided figure that has three  
275 angles] causes [*M* outputs *W* at *t*<sub>3</sub>].

276 However using the above background, we can now give the following argu-  
277 ment from causal exclusion that (ANGLE<sub>t<sub>1</sub></sub>) is instead false: Just as [at *t*<sub>2</sub>, *W* is  
278 a closed straight-sided figure that has three angles] fails to cause the closed  
279 straight-sided figure detector to output *W* at *t*<sub>3</sub> (since the former fact goes  
280 beyond what is causally relevant), [at *t*<sub>1</sub>, *W* is a closed straight-sided figure  
281 that has three angles] fails to cause the closed straight-sided figure detector  
282 to output *W* (since this fact also goes beyond what is causally relevant) and  
283 hence this fact fails to cause [*W* is in the three-angle detector at *t*<sub>2</sub>]. Hence we  
284 have (8).

285 (8) [at *t*<sub>1</sub>, *W* is a closed straight-sided figure that has three angles] does not  
286 cause [*W* is in the three angle detector at *t*<sub>2</sub>].

287 Similarly, while [*W* has three angles at *t*<sub>1</sub>] is a cause of [*W* has three angles  
288 at *t*<sub>2</sub>], it is not the case that [at *t*<sub>1</sub>, *W* is a closed straight-sided figure that has  
289 three angles] causes this fact, since it goes beyond what is causally relevant.  
290 Hence we have (9).

291 (9) [at *t*<sub>1</sub>, *W* is a closed straight-sided figure that has three angles] does not  
292 cause [*W* has three angles at *t*<sub>2</sub>].

293 Since [at *t*<sub>1</sub>, *W* is a closed straight-sided figure that has three angles] is also  
294 not caused by either [*W* is in the three-angle detector at *t*<sub>2</sub>] or [*W* has three  
295 angles at *t*<sub>2</sub>], and the causal chain that leads up to [*M* outputs *W* at *t*<sub>3</sub>] goes  
296 through [*W* is in the three-angle detector at *t*<sub>2</sub>] and [*W* has three angles at *t*<sub>2</sub>],  
297 it therefore follows from (8) and (9) that [at *t*<sub>1</sub>, *W* is a closed straight-sided  
298 figure that has three angles] isn't part of the causal chain that leads to [*M*  
299 outputs *W* at *t*<sub>3</sub>] and hence does not cause it. Hence (ANGLE<sub>t<sub>1</sub></sub>) is false.

300  $ANGLE_{t_1}$ . [At  $t_1$ ,  $W$  is a closed straight-sided figure that has three  
301 angles] causes [ $M$  outputs  $W$  at  $t_3$ ].

302 A more rigorous version of the above argument against ( $ANGLE_{t_1}$ ) can be  
303 given by appealing to the version of the principle of causal exclusion given by  
304 ( $PCE$ ).<sup>11</sup>

305  $PCE$ . In cases where there is no genuine causal overdetermination,  
306 if  $S$  is a set of facts that occur at a time  $t$  whose members collectively  
307 completely cause  $f$ , then  $S$  is the unique set of facts that occur at  $t$   
308 and collectively completely cause  $f$ .

309 In ( $PCE$ ), a fact is said to occur at a certain time iff the fact only concerns  
310 how things are at that time. Genuine causal overdeterminism, on the other  
311 hand, occurs when two independent causal processes converge on the same  
312 effect, such as when a house burns down because a lit match starts a fire in  
313 the garbage at the same time as lightning strikes the house.

314 Since there is no genuine causal overdetermination in the case of  $W$  being  
315 outputted by  $M$ , ( $PCE$ ) can be used to argue that ( $ANGLE_{t_1}$ ) is false as follows:  
316 Suppose, for reductio, that ( $ANGLE_{t_1}$ ) is true. Then [ $W$  is a closed straight-  
317 sided figure that has three angles at  $t_1$ ] together with the members of some  
318 possibly empty set  $\Psi_1$  completely cause [ $M$  outputs  $W$  at  $t_3$ ]. Since ( $ANGLE_{t_1}^*$ )  
319 holds, it is also true that [ $W$  is a closed straight-sided figure at  $t_1$ ], [ $W$  has  
320 three angles at  $t_1$ ] together with the members of some possibly empty set  $\Psi_2$   
321 collectively completely cause [ $M$  outputs  $W$  at  $t_3$ ]. Since the relevant facts  
322 occur at the same time, these two consequences together with ( $PCE$ ) then  
323 entail (10).

324 (10) [ $W$  is a closed straight-sided figure at  $t_1$ ], [ $W$  has three angles at  $t_1$ ], [ $W$   
325 is a closed straight-sided figure that has three angles] and the members  
326 of some possibly empty set  $\Psi$  collectively completely cause [ $M$  outputs  
327  $W$  at  $t_3$ ].

328 If (10) is true, then [ $W$  is a closed straight-sided figure at  $t_1$ ], [ $W$  has three  
329 angles at  $t_1$ ] and the members of  $\Psi$  by themselves collectively completely  
330 cause [ $M$  outputs  $W$  at  $t_3$ ], since [at  $t_1$ ,  $W$  is closed straight-sided figure that

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11 For discussion of the principle of causal exclusion, see, for example, Kim (2005) and Moore (2018).

331 has three angles] is superfluous given the presence of [ $W$  is a closed straight-  
 332 sided figure at  $t_1$ ] and [ $W$  has three angles at  $t_1$ ]. Given (PCE), however, this  
 333 consequence conflicts with (10). Hence, the reductio assumption (ANGLE $_{t_1}$ )  
 334 is false.

335 The above argument shows that (ANGLE $_{t_1}$ ) fails to hold if (PCE) holds. Not  
 336 all philosophers, however, accept (PCE), and these philosophers will not be  
 337 convinced by the above argument from causal exclusion that the dual-detector  
 338 argument fails. For example, some philosophers reject (PCE) on the grounds  
 339 that it conflicts with the popular counterfactual dependency thesis (DEP).<sup>12</sup>

340 DEP. Suppose that  $f$  and  $g$  obtain, and that, had  $f$  failed to obtain,  
 341 it would have been that  $g$  failed to obtain. Then,  $f$  causes  $g$ .

342 Other philosophers reject (PCE) because they hold that, in cases where there  
 343 is no genuine causal overdetermination of a fact, there can still be multiple  
 344 complete causal chains that converge on that fact, provided these chains  
 345 are systematically related to each other in the right way. In particular, some  
 346 philosophers hold that there can be multiple such causal chains provided that,  
 347 for each such chain, either that chain generates all the other chains, or that  
 348 chain is generated by at least one other such chain. Someone who endorses  
 349 this view, for example, might endorse (CONJ).<sup>13</sup>

350 CONJ. If  $f_1$  and  $f_2$  together with the members of a set  $\Phi$  collectively  
 351 completely cause  $f$ , then the conjunction of  $f_1$  and  $f_2$  together with  
 352 the members of  $\Phi$  collectively completely cause  $f$ .

353 It follows from (CONJ) that, contra (PCE), if there is one causal chain leading  
 354 to  $f$  that contains the facts  $f_1$  and  $f_2$  occurring at a time  $t$ , then there is a further  
 355 causal chain which is systematically related to it by virtue of containing the  
 356 conjunction of  $f_1$  and  $f_2$  instead of  $f_1$  and  $f_2$  themselves. Given (CONJ), it is  
 357 natural to hold that this further causal chain containing the conjunction of  $f_1$   
 358 and  $f_2$  is generated by the former chain containing its conjuncts.

12 See, for example, Loewer (2007). Proponents of (DEP) typically place certain restrictions on (DEP), such as requiring that the counterfactual is to be read in a suitable non-backtracking sense (see Lewis 1973), that the facts (or events, when (DEP) is applied to events) that stand in the causation relation are “sufficiently distinct” (so that, for example, we don’t have the consequence that each fact causes itself) (see Kim 1973; Lewis 1986c), and that these facts (or events) are non-disjunctive (see Lewis 1986c).

13  $\Phi$  in (CONJ) can be the empty set.

359 In light of the above views, the argument from causal exclusion does not by  
 360 itself decisively refute the  $t_1$ -version of the dual-detector argument. In addition  
 361 to facing the argument from causal exclusion, however, the  $t_1$ -version of the  
 362 dual-detector argument faces the problem that, even if the causal exclusion  
 363 argument fails, it doesn't appear possible to justify the truth of ( $\text{ANGLE}_{t_1}$ )  
 364 while also justifying the falsity of ( $\text{SIDE}_{t_1}$ ). (Or at least, it doesn't seem possible  
 365 to do this without relying on some other argument against the modal theory  
 366 which, if successful, would by itself refute the modal theory. I will discuss two  
 367 attempts to give such a justification, and I will argue that both these attempts  
 368 fail. The failure of these two attempts will give us reason to think that no such  
 369 justification is possible, and hence reason to think that, even if ( $\text{PCE}$ ) and  
 370 the argument from causal exclusion fail, the  $t_1$ -version of the dual-detector  
 371 argument is still unsuccessful.

372 The first attempt to justify the truth of ( $\text{ANGLE}_{t_1}$ ) (while also justifying  
 373 the falsehood of ( $\text{SIDE}_{t_1}$ ) appeals to ( $\text{CONJ}$ ) above. This first attempt accepts  
 374 ( $\text{ANGLE}_{t_1}^*$ ) on the basis of the transitivity reasoning given for it above. It then  
 375 infers from ( $\text{ANGLE}_{t_1}^*$ ) and ( $\text{CONJ}$ ) that the conjunction of [ $W$  is a closed  
 376 straight-sided figure at  $t_1$ ] and [ $W$  has three angles at  $t_1$ ] collectively (partially)  
 377 cause  $M$  to output  $W$  at  $t_3$ . Assuming (as I will from now on) that this con-  
 378 junction is the fact [at  $t_1$ ,  $W$  is a closed straight-sided figure that has three  
 379 angles], it follows from this that ( $\text{ANGLE}_{t_1}$ ) is true.

380  $\text{ANGLE}_{t_1}$ . [At  $t_1$ ,  $W$  is a closed straight-sided figure that has three  
 381 *angles*] causes [ $M$  outputs  $W$  at  $t_3$ ].

382 Let us assume that the above justification of ( $\text{ANGLE}_{t_1}$ ) is successful. The  
 383 question that now needs to be addressed is whether we can go on to justify  
 384 the falsehood of ( $\text{SIDE}_{t_1}$ ).

385  $\text{SIDE}_{t_1}$ . [At  $t_1$ ,  $W$  is a closed straight-sided figure that has three *sides*]  
 386 causes [ $M$  outputs  $W$  at  $t_3$ ].

387 One argument that tries to justify the falsehood of ( $\text{SIDE}_{t_1}$ ) is the following:  
 388 Unlike ( $\text{ANGLE}_{t_1}$ ), ( $\text{SIDE}_{t_1}$ ) cannot be generated from the causal facts given to  
 389 us in the description of  $M$  processing  $W$  given in the dual-detector argument  
 390 using causal generational principles such as ( $\text{T}$ ) and ( $\text{CONJ}$ ). As a result, the  
 391 truth of ( $\text{SIDE}_{t_1}$ ) would require some additional primitive causal fact to hold  
 392 in the case of  $M$  processing  $W$ , which would be unparsimonious. Moreover,

393 since any such additional primitive causal fact would only contingently hold,  
 394 the possibility of such a fact holding can be removed by simply stipulating  
 395 that no such additional primitive causal fact holds in the possible case of *M*  
 396 processing *W* that we are concerned with. Hence, according to this argument,  
 397 the truth of (*SIDE*<sub>*t*<sub>1</sub></sub>) can be ruled out either on parsimony grounds or by  
 398 stipulation.

399 The problem with this argument for the falsity of (*SIDE*<sub>*t*<sub>1</sub></sub>) is that it begs the  
 400 question against the modal theory. It does this because, if the modal theory  
 401 is true, then, contra the above argument, (*SIDE*<sub>*t*<sub>1</sub></sub>) can be generated from the  
 402 causal facts given to us in the description of the case of *M* processing *W* in the  
 403 dual-detector argument and the generational principles (*T*) and (*CONJ*) in the  
 404 same way that (*ANGLE*<sub>*t*<sub>1</sub></sub>) can be so generated. This is because, if the modal  
 405 theory is true, then [at *t*<sub>1</sub>, *W* is a closed straight-sided figure that has three  
 406 sides] is the conjunction of [*W* is a closed straight-sided figure at *t*<sub>1</sub>] and [*W*  
 407 has three angles at *t*<sub>1</sub>], just as much as [at *t*<sub>1</sub>, *W* is a closed straight-sided figure  
 408 that has three angles] is. Hence, if the modal theory is true, then (*SIDE*<sub>*t*<sub>1</sub></sub>) can  
 409 be derived from (*ANGLE*<sub>*t*<sub>1</sub></sub><sup>\*</sup>) and (*CONJ*) in the same way that (*ANGLE*<sub>*t*<sub>1</sub></sub>) can.

410 An alternative way of trying to justify the falsehood of (*SIDE*<sub>*t*<sub>1</sub></sub>) appeals to  
 411 (*CONJ*<sup>\*</sup>).<sup>14</sup>

412 *CONJ*<sup>\*</sup>. If the conjunction of *f*<sub>1</sub> and *f*<sub>2</sub> partially causes *f*, then *f*<sub>1</sub>  
 413 and *f*<sub>2</sub> collectively partially cause *f*.

414 We can give the same kind of argument from parsimony and contingency for  
 415 the falsity of (*SIDE*<sub>*t*<sub>1</sub></sub><sup>\*</sup>) as was given above for the falsity of (*SIDE*<sub>*t*<sub>1</sub></sub>), with the  
 416 difference that this argument for the falsity of (*SIDE*<sub>*t*<sub>1</sub></sub><sup>\*</sup>), unlike the argument  
 417 for the falsity of (*SIDE*<sub>*t*<sub>1</sub></sub>), does not beg the question against the modal theory.

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14 (*CONJ*) and (*CONJ*<sup>\*</sup>) are in the vicinity of two principles, (*A*) and (*B*), that Sober appeals to when defending the dual-detector argument.

A. If two devices, “which are linked in series in the [machine], are sensitive just to properties *P* and *Q*, respectively, then the [machine] itself is sensitive to the conjunctive property *P*-and-*Q*.” (Sober 1982, 186)

B. If “two devices which are linked in series are such that the first is sensitive to *P* and the second is *not* sensitive to *R* (where *P* ≠ *R*, and neither implies the other), then the [machine] is *not* sensitive to the conjunctive property *P*-and-*R*.” (Sober 1982, 186)

As argued below in the case of (*CONJ*<sup>\*</sup>), (*B*) immediately conflicts with the modal theory and is hard to justify.



418  $\text{SIDE}_{t_1}^*$ . [ $W$  is a closed straight-sided figure at  $t_1$ ] and [ $W$  has three  
419 sides at  $t_1$ ] collectively cause [ $M$  outputs  $W$  at  $t_3$ ].

420 Indeed, plausibly both opponents and proponents of the modal theory should  
421 reject ( $\text{SIDE}_{t_1}^*$ ). Given the falsity of ( $\text{SIDE}_{t_1}^*$ ), however, the falsity of ( $\text{SIDE}_{t_1}$ )  
422 follows from ( $\text{CONJ}^*$ ).<sup>15</sup> If we are justified in endorsing ( $\text{CONJ}^*$ ), then, we can  
423 use it to justify the falsehood of ( $\text{SIDE}_{t_1}$ ).

424 One problem with ( $\text{CONJ}^*$ ) is that the principle directly conflicts with the  
425 modal theory. This is because, if the modal theory holds, then ( $\text{CONJ}^*$ ) has  
426 the absurd consequence that, if  $f$  partially causes  $g$ , then any fact  $h$  that  
427 is necessitated by  $f$  also causes  $g$ . (This is because, according to the modal  
428 theory, if a fact  $f$  necessitates a fact  $h$ , then  $f$  is the conjunction of  $f$  and  
429  $h$ .) If [Suzy throws a rock] causes [the window breaks], for example, then,  
430 if the modal theory holds, ( $\text{CONJ}^*$ ) entails that [Suzy throws a rock or Suzy  
431 does not throw a rock] (which is necessitated by [Suzy throws a rock]) also  
432 causes [the window breaks], which is absurd. In light of this, one problem  
433 with ( $\text{CONJ}^*$ ) is that, if it is accepted, then we don't need the dual-detector  
434 argument to refute the modal theory, since ( $\text{CONJ}^*$ ) by itself achieves this  
435 task. If the dual-detector argument needs to rely on ( $\text{CONJ}^*$ ) in order to be  
436 successful, then, the argument is superfluous.

437 A second (more serious) problem with ( $\text{CONJ}^*$ ) is that it is not clear why  
438 we should believe it. A proponent of ( $\text{CONJ}^*$ ) might attempt to justify the  
439 principle by arguing that, in ordinary language, sentences of the form (11)  
440 are equivalent to sentences of the form (12).

- 441 (11)  $\varphi$  because  $\phi$  and  $\psi$ .  
442 (12)  $\varphi$  because  $\phi$  and because  $\psi$ .

443 Such a proponent might then argue that (on its relevant causal use) (11) is  
444 equivalent to (11\*) and (12) is equivalent to (12\*).

- 445 (11\*) [ $\phi$  and  $\varphi$ ] causes [ $\varphi$ ].  
446 (12\*) [ $\phi$  and  $\varphi$ ] collectively cause [ $\varphi$ ].

447 Assuming that these equivalences all hold, it follows that (11\*) entails (12\*),  
448 from which it follows that ( $\text{CONJ}^*$ ) holds.

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15 I am assuming that [at  $t_1$ ,  $W$  is a closed straight-sided figure that has three sides] is the conjunction of [ $W$  is a closed straight-sided figure at  $t_1$ ] and [ $W$  has three sides at  $t_1$ ].

449 A problem with this attempted justification for (CONJ\*) is that (12) is plausi-  
 450 bly ambiguous between a conjunctive reading and a non-conjunctive reading,  
 451 just like (13) is (cf. Marshall 2021, 8035).

452 (13) Jane wants to go swimming and go hiking.

453 (13) has a non-conjunctive reading on which the proposition Jane is described  
 454 as desiring is the proposition that Jane goes swimming and hiking. On this  
 455 reading, (13) is true iff (13n) is true.

456 (13n) Jane wants to go (swimming and hiking).

457 (13) also has a conjunctive reading on which (13) is true iff (13c) is true.

458 (13c) Jane wants to go swimming and Jane wants to go hiking.

459 (11) is plausibly similarly ambiguous between a non-conjunctive reading  
 460 on which it is equivalent to (11n) and a conjunctive reading on which it is  
 461 equivalent to (11c).

462 (11n)  $\varphi$  because ( $\phi$  and  $\psi$ ).

463 (11c) ( $\varphi$  because  $\phi$ ) and ( $\varphi$  because  $\psi$ ).

464 On its conjunctive reading, while (11) is equivalent to ((12) (on its causal use),  
 465 there is no reason to think that (on its causal use) (11) is equivalent to (11\*)  
 466 (or at least no such reason has yet been provided).<sup>16</sup> On its non-conjunctive  
 467 reading, on the other hand, there is no reason to think that (11) is equivalent  
 468 to (12). As a result, appealing to natural language does not appear to help a  
 469 proponent of the dual-detector argument justify (CONJ\*). In light of this, it  
 470 is not clear how (CONJ\*) might be justified.<sup>17</sup> As a result, it does not appear  
 471 possible to justify the truth of (ANGLE<sub>t<sub>1</sub></sub>) by appealing to (CONJ) while also  
 472 justifying the falsity of (SIDE<sub>t<sub>1</sub></sub>).

16 The claim that (12) is equivalent to (12\*) can also be resisted, since it might be denied that 'f causes h' and 'g causes h' entails 'f and g collectively cause h'. For example, this inference might be thought to fail if f and g are individually complete causes of h that concern different times.

17 Or at least, it is not clear how (CONJ\*) might be justified without begging the question against the modal theory. It might perhaps be possible to justify (CONJ\*) if we assume the structured theory and give a general account of how less fundamental facts get to have their causal features in terms of the causal features of more fundamental facts that involves principles like (CONJ).

473 I will discuss one further attempt to justify both the truth of (**ANGLE**<sub>*t*<sub>1</sub></sub>) and  
 474 the falsity of (**SIDE**<sub>*t*<sub>1</sub></sub>). Instead of appealing to (**CONJ**), this second attempt  
 475 appeals to the popular counterfactual dependency thesis (**DEP**) stated above.<sup>18</sup>

476 DEP. Suppose that *f* and *g* obtain, and that, had *f* failed to obtain,  
 477 it would have been that *g* failed to obtain. Then, *f* causes *g*.

478 Assuming that (**DEP**) holds, we can derive (**ANGLE**<sub>*t*<sub>1</sub></sub>) as follows: In the case  
 479 of *M* outputting *W*, had it not been that, at *t*<sub>1</sub>, *W* was a closed straight-sided  
 480 figure that had three *angles*, then either: i) *W* would not have been a closed  
 481 straight-sided figure at *t*<sub>1</sub>; or ii) *W* would not have had three angles at *t*<sub>1</sub>, in  
 482 which case *W* would also not have had three angles at *t*<sub>2</sub>. If *W* had failed to be  
 483 a closed straight-sided figure at *t*<sub>1</sub>, *W* would not have been outputted by the  
 484 closed straight-sided figure detector at *t*<sub>2</sub>, and hence *W* would not have been  
 485 outputted by *M* at *t*<sub>3</sub>. On the other hand, if *W* had failed to have three angles  
 486 at *t*<sub>2</sub>, it would not have been outputted by the three-angle detector at *t*<sub>3</sub>, and  
 487 hence would also not have been outputted by *M* at *t*<sub>3</sub>. Hence, had it not been  
 488 that, at *t*<sub>1</sub>, *W* was a closed straight-sided figure that had three *angles*, *M* would  
 489 not have outputted *W* at *t*<sub>3</sub>. It therefore follows from (**DEP**) that (**ANGLE**<sub>*t*<sub>1</sub></sub>) is  
 490 true.

491 ANGLE<sub>*t*<sub>1</sub></sub>. [At *t*<sub>1</sub>, *W* is a closed straight-sided figure that has three  
 492 *angles*] causes [*M* outputs *W* at *t*<sub>3</sub>].

493 Assuming that (**DEP**) holds, then, a proponent of the dual-detector argument  
 494 can use (**DEP**) to justify (**ANGLE**<sub>*t*<sub>1</sub></sub>). Unfortunately for proponents of the dual-  
 495 detector argument, however, if (**DEP**) holds it can also be used to justify the  
 496 truth of (**SIDE**<sub>*t*<sub>1</sub></sub>). To see why, note that, had it not been that, at *t*<sub>1</sub>, *W* was a  
 497 closed straight-sided figure that had three *sides*, then *W* would also either:  
 498 i) not have been a closed straight-sided figure at *t*<sub>1</sub> or ii) not have had three  
 499 angles at *t*<sub>1</sub>, in which case it would not have had three angles at *t*<sub>2</sub>. Hence, had  
 500 it not been that, at *t*<sub>1</sub>, *W* was a closed straight-sided figure having three *sides*,  
 501 at least one of the detectors would not have outputted *W*, and so *M* would  
 502 not have outputted *W* at *t*<sub>3</sub>. Hence, it also follows from (**DEP**) that (**SIDE**<sub>*t*<sub>1</sub></sub>)  
 503 is true. Hence, a proponent of the dual-detector argument cannot use (**DEP**)

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18 Related principles we might try to appeal to in order to simultaneously justify the truth of (**ANGLE**) and the falsity of (**SIDE**) (which have similar problems to (**DEP**)) are difference-making principles, such as those proposed by Sartorio (2005) and List and Menzies (2009).

504 to justify the combination of ( $\text{ANGLE}_{t_1}$ ) being true and ( $\text{SIDE}_{t_1}$ ) being false.  
 505 This second attempt at justifying the truth of ( $\text{ANGLE}_{t_1}$ ) and the falsehood of  
 506 ( $\text{SIDE}_{t_1}$ ) therefore fails.

507 I have now discussed two attempts to justify the truth of ( $\text{ANGLE}_{t_1}$ ) and the  
 508 falsity of ( $\text{SIDE}_{t_1}$ ), and I have argued that both of these attempts fail. As far as  
 509 I can see, other attempts to do this are equally unsuccessful. If this is the case,  
 510 then both the  $t_1$ -version and the  $t_2$ -version of the dual-detector argument fail.

### 513 Variants of the Dual-Detector Argument

512 In the face of the failure of the original version of Sober's dual-detector argu-  
 513 ment, it might be thought that the argument can be modified so that it evades  
 514 the problems discussed in section 2. In particular, it might be thought that  
 515 these problems can be evaded by replacing the necessarily equivalent facts  
 516 expressed by ( $1t_1$ ) and ( $2t_1$ ) with some other necessarily equivalent facts and  
 517 describing a machine that is causally sensitive to one of these facts but not  
 518 the other.

519 ( $1t_1$ )  $W$  is a closed straight-sided figure that has three *angles* at  $t_1$ .

520 ( $2t_1$ )  $W$  is a closed straight-sided figure that has three *sides* at  $t_1$ .

521 As far as I can see, however, this cannot be done.

522 To illustrate the difficulty involved in successfully modifying the dual-  
 523 detector argument in the above manner, I will briefly consider two attempts  
 524 to do this that replace the facts expressed by ( $1t_1$ ) and ( $2t_1$ ) with the facts  
 525 expressed by (14) and (15), where  $W^*$  is a circular wire and where the facts  
 526 expressed by (14) and (15) are both necessarily equivalent to the fact that  $W^*$   
 527 is a circle.<sup>19</sup>

528 (14)  $W^*$  is a closed (plane) figure all of whose points are equidistant from a  
 529 point.

530 (15)  $W^*$  is a closed (plane) figure of constant curvature.

531 For the first attempt, consider a machine  $M_1^*$  that, when given a closed (plane)  
 532 figure as an input, scans that figure by having a distinct curvature detector for  
 533 each point of the figure. Suppose that each of these detectors measures the  
 534 curvature of their associated point in the figure and sends the result of this  
 535 measurement in the form of a signal to the CPU of  $M_1^*$ . Further, suppose that,

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19 This variant was suggested by a referee.

536 if all the signals the CPU receives are of the same value, then the fact that the  
 537 signals it receives have the same value causes the figure to be outputted by  
 538  $M_1^*$ . Finally, suppose that the circular wire  $W^*$  is inputted into this machine  
 539  $M_1^*$ , is scanned by it, and is then outputted by it. It might then be claimed that,  
 540 in this case, (CURV) is true while (DIST) is false, and that, due to Leibniz's law,  
 541 this difference in truth-value entails that the modal theory is false.

542 CURV. [ $W^*$  is a closed figure with constant curvature] causes [ $M_1^*$   
 543 outputs  $W^*$ ].

544 DIST. [ $W^*$  is a closed figure all of whose points are equidistant from  
 545 a point] causes [ $M_1^*$  outputs  $W^*$ ].

546 A problem with this first attempt at finding a successful variant of the dual-  
 547 detector argument is that it is no more obvious that (CURV) holds than it is  
 548 that (ANGLE $_{t_1}$ ) holds in Sober's original case.

549 ANGLE $_{t_1}$ . [At  $t_1$ ,  $W$  is a closed straight-sided figure that has three  
 550 angles] causes [ $M$  outputs  $W$  at  $t_3$ ].

551 Instead, using transitivity reasoning, what can be uncontroversially estab-  
 552 lished in the variant case of machine  $M_1^*$  is a claim along the lines of (CURV\*),  
 553 just as what can be uncontroversially established using such reasoning in  
 554 Sober's original case of machine  $M$  is (ANGLE\* $_{t_1}$ ).

555 CURV\*. [Point  $p_1$  of  $W^*$  has curvature  $C$ ], [point  $p_2$  of  $W^*$  has  
 556 curvature  $C$ ]... collectively cause [ $M_1^*$  outputs  $W^*$ ].

557 ANGLE\* $_{t_1}$ . [ $W$  is a closed straight-sided figure at  $t_1$ ] and [ $W$  has three  
 558 angles at  $t_1$ ] collectively cause [ $M$  outputs  $W$  at  $t_3$ ].

559 Moreover, an opponent of the modal theory who wishes to show that (CURV)  
 560 and (DIST) differ in their truth-value faces the same challenges that a pro-  
 561 ponent of Sober's original version of the dual-detector argument faces in  
 562 showing that (ANGLE $_{t_1}$ ) and (SIDE $_{t_1}$ ) differ in their truth-value. First, they  
 563 need to resist an argument from causal exclusion that (CURV\*) entails the  
 564 falsehood of (CURV). And second, they need to find some way of justifying the  
 565 truth of (CURV) while also justifying the falsehood of (DIST), a task that ap-  
 566 pears to be just as difficult as finding a way of justifying the truth of (ANGLE $_{t_1}$ )

567 while also justifying the falsehood of ( $\text{SIDE}_{t_1}$ ). Hence, this first attempt at  
568 describing a machine that is differentially sensitive to the facts expressed by  
569 (14) and (15) results in a variant of the dual-detector argument that is no more  
570 successful than Sober's original argument.

571 For a second attempt to show that there could be a machine that is causally  
572 sensitive to one of the facts expressed by (14) and (15) but not the other,  
573 consider a machine  $M_2^*$  that contains an extendable straight rod that rotates  
574 around one of its endpoints. When given a closed figure as input,  $M_2^*$  works  
575 by placing this rod inside the inputted closed figure, fixing the location of  
576 one of the rod's endpoints, extending the length of the rod until its other  
577 endpoint touches the inputted figure, and then rotating the rod around its  
578 fixed endpoint while keeping the length of the rod fixed. If the rod does a full  
579 rotation without moving the inputted figure or losing touch with it, then the  
580 fact that it does this causes  $M_2^*$  to output the figure. Suppose now that the  
581 circular wire  $W^*$  is inputted into  $M_2^*$  and that the rod of  $M_2^*$  is placed inside  
582 of  $W^*$  and does a full rotation meeting the above conditions, so that  $W^*$  gets  
583 outputted by  $M_2^*$ . It might then be claimed that, in this case, ( $\text{DIST}$ ) is true  
584 and ( $\text{CURV}$ ) is false, and hence that the modal theory is false.

585 The problem with this second variant of Sober's version of the dual-detector  
586 argument is that, if  $W^*$  is a circle that is inputted into and then outputted by  
587  $M_2^*$ , then there is no reason to think that ( $\text{CURV}$ ) and ( $\text{DIST}$ ) differ in their  
588 truth-value. In particular, if  $W^*$  is so inputted and outputted, it is equally  
589 plausible to say that the machine measures the curvature of the points of  $W^*$   
590 as it is to say that it measures the equidistance of those points from a common  
591 point. After all, the rod would fail to do its full rotation (while touching but  
592 not moving  $W^*$ ) if the points of  $W^*$  didn't have constant curvature, just as it  
593 would fail to do this if the points of  $W^*$  weren't equally distant from some  
594 common point. There is therefore no grounds for thinking that  $W^*$  being  
595 outputted by  $M_2^*$  is due to one of these facts rather than the other. Hence,  $M_2^*$   
596 also fails to be a demonstrable case of a machine that is causally sensitive to  
597 one of the facts expressed by (14) and (15) and not the other.

598 Other variations of Sober's original version of the dual-detector argument  
599 face similar problems to those described above. Indeed, the above two attempts  
600 to construct a successful variant of Sober's original version of the argument  
601 arguably illustrate a dilemma facing any such attempt. This dilemma is the  
602 following: Suppose we have a machine whose output is intended to be caused  
603 by the fact  $f_1$  and not by the necessarily equivalent fact  $f_2$ . Then the machine  
604 will either contain multiple detectors that differ in what aspects of the input

605 they measure (as in the cases of  $M$  and  $M_1^*$ ), or the machine will only contain  
 606 detectors (or a single detector) that don't so differ (as in the case of  $M_2^*$ ). If  
 607 the machine contains multiple detectors that differ in what aspects of the  
 608 input they measure, then the argument against the modal theory based on  
 609 this machine will arguably face the same challenges facing Sober's original arg-  
 610 ument and the first variant of it discussed above. In particular, the argument  
 611 will need to resist an argument from causal exclusion and will face the same  
 612 difficulties in justifying the claim that the input being outputted is caused by  
 613  $f_1$  and not by  $f_2$  that Sober's original dual-detector argument faces in justifying  
 614 the truth of ( $ANGLE_{t_1}$ ) and the falsity of ( $SIDE_{t_1}$ ). On the other hand, if the  
 615 machine contains only a single detector (or multiple detectors that don't differ  
 616 in what aspects of the input they measure), then it will arguably fail to be  
 617 even initially plausible that  $f_1$  and  $f_2$  differ in whether they cause the input  
 618 to be outputted just as there is no even initial plausibility for thinking that  
 619 the facts expressed by (14) and (15) differ in whether they cause  $W^*$  to be  
 620 outputted by machine  $M_2^*$ . Hence, whether or not we have a machine that  
 621 contains detectors that differ in what aspects they measure, the argument  
 622 against the modal theory based on this machine will arguably fail. In light of  
 623 this, it is reasonable to conclude that, not only does Sober's original version of  
 624 the dual-detector argument fail, but it is not possible to modify the argument  
 625 so that it is successful. If this is correct, then all variants of the dual-detector  
 626 argument fail and some other kind of argument will be needed if we are to  
 627 have reason to reject the modal theory of facts and properties.\*

628 Dan Marshall

629  0000-0002-5763-3875

630 Lingnan University

631 danmarshall@ln.edu.hk

## 632 References

- 633 ACHINSTEIN, Peter. 1974. "The Identity of Properties." *American Philosophical Quar-*  
 634 *terly* 11(4): 257–275.
- 635 ARMSTRONG, David M. 1997. *A World of States of Affairs*. Cambridge: Cambridge  
 636 University Press, doi:10.1017/cbo9780511583308.

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- 637 AUDI, Paul. 2016. "Property Identity." *Philosophy Compass* 11(12): 829–840, doi:10.1111  
638 1/phc3.12380.
- 639 BJERRING, Jens Christian and SCHWARZ, Wolfgang. 2017. "Granularity Problems."  
640 *The Philosophical Quarterly* 67(266): 22–37, doi:10.1093/pq/pqw028.
- 641 BRAUN, David. 1998. "Understanding Belief Reports." *The Philosophical Review* 107(4):  
642 555–595, doi:10.2307/2998375.
- 643 DORR, Cian. 2016. "To Be *F* Is to Be *G*." in *Philosophical Perspectives 30: Metaphysics*,  
644 edited by John HAWTHORNE and Jason TURNER, pp. 39–134. Hoboken, New Jersey:  
645 John Wiley and Sons, Inc., doi:10.1111/phpe.12079.
- 646 ENÇ, Berent. 1982. "Intentional States of Mechanical Devices." *Mind* 91(362): 161–183,  
647 doi:10.1093/mind/xci.362.161.
- 648 GOODMAN, Jeremy. 2017. "Reality Is Not Structured." *Analysis* 77(1): 43–53, doi:10.1  
649 093/analys/anw002.
- 650 HALL, Ned. 2000. "Causation and the Price of Transitivity." *The Journal of Philosophy*  
651 97(4): 198–222, doi:10.2307/2678390.
- 652 JACKSON, Frank. 1998. *From Metaphysics to Ethics: A Defense of Conceptual Analysis*.  
653 Oxford: Oxford University Press, doi:10.1093/0198250614.001.0001.
- 654 KIM, Jaegwon. 1973. "Causes and Counterfactuals." *The Journal of Philosophy* 70(17):  
655 570–572, doi:10.2307/2025312.
- 656 —. 2005. *Physicalism, or Something Near Enough*. Princeton Monographs in Philosophy  
657 n. 19. Princeton, New Jersey: Princeton University Press, doi:10.1515/9781400840  
658 847.
- 659 KMENT, Boris. 2022. "Russell-Myhill and Grounding." *Analysis* 82(1): 49–60, doi:10.1  
660 093/analys/anab028.
- 661 KVART, Igal. 1991. "Transitivity and Preemption of Causal Relevance." *Philosophical*  
662 *Studies* 64(2): 125–160, doi:10.1007/bf00404826.
- 663 LEWIS, David. 1973. "Causation." *The Journal of Philosophy* 70(17): 556–567. Reprinted,  
664 with a postscript (Lewis 1986d), in Lewis (1986b, 159–172), doi:10.2307/2025310.
- 665 —. 1986a. *On the Plurality of Worlds*. Oxford: Blackwell Publishers.
- 666 —. 1986b. *Philosophical Papers, Volume 2*. Oxford: Oxford University Press, doi:10.109  
667 3/0195036468.001.0001.
- 668 —. 1986c. "Events." in *Philosophical Papers, Volume 2*, pp. 241–270. Oxford: Oxford  
669 University Press, doi:10.1093/0195036468.003.0008.
- 670 —. 1986d. "Postscript to Lewis (1973)." in *Philosophical Papers, Volume 2*, pp. 172–213.  
671 Oxford: Oxford University Press, doi:10.1093/0195036468.003.0006.
- 672 LIST, Christian and MENZIES, Peter. 2009. "Nonreductive Physicalism and the Limits  
673 of the Exclusion Principle." *The Journal of Philosophy* 106(9): 475–502, doi:10.584  
674 0/jphil2009106936.
- 675 LOEWER, Barry C. 2007. "Mental Causation, or Something Near Enough." in *Con-*  
676 *temporary Debates in Philosophy of Mind*, edited by Brian P. MCLAUGHLIN and



- Jonathan COHEN, pp. 243–264. *Contemporary Debates in Philosophy* n. 8. Oxford: Blackwell Publishers. Second edition: McLaughlin and Cohen (2023).
- MARSHALL, Dan. 2021. “Causation and Fact Granularity.” *Synthese* 199(3-4): 8029–8045, doi:10.1007/s11229-021-03151-2.
- MCDERMOTT, Michael. 1995. “Redundant Causation.” *The British Journal for the Philosophy of Science* 46(4): 523–544, doi:10.1093/bjps/46.4.523.
- MCKAY, Thomas J. and NELSON, Michael. 2010. “Propositional Attitude Reports.” in *The Stanford Encyclopedia of Philosophy*. Stanford, California: The Metaphysics Research Lab, Center for the Study of Language and Information, <https://plato.stanford.edu/archives/win2010/entries/prop-attitude-reports/>.
- MCLAUGHLIN, Brian P. and COHEN, Jonathan, eds. 2007. *Contemporary Debates in Philosophy of Mind*. Contemporary Debates in Philosophy n. 8. Oxford: Blackwell Publishers. Second edition: McLaughlin and Cohen (2023).
- , eds. 2023. *Contemporary Debates in Philosophy of Mind*. 2nd ed. Contemporary Debates in Philosophy n. 8. Hoboken, New Jersey: Wiley-Blackwell. First edition: McLaughlin and Cohen (2007), doi:10.1002/9781394259847.
- MILLER, Alexander. 1995. “Objectivity Disfigured: Mark Johnston’s Missing-Explanation Argument.” *Philosophy and Phenomenological Research* 55(4): 857–868, doi:10.2307/2108336.
- MOLNAR, George. 2003. *Powers: A Study in Metaphysics*. Oxford: Oxford University Press. Edited by Stephen Mumford, doi:10.1093/acprof:oso/9780199204175.001.0001.
- MOORE, Dwayne. 2018. “Mind and the Causal Exclusion Problem.” in *Internet Encyclopedia of Philosophy*. University of Tennessee at Martin, <https://iep.utm.edu/mind-and-the-causal-exclusion-problem/>.
- PARTEE, Barbara Hall. 1989. “Possible Worlds in Model-Theoretic Semantics: A Linguistic Perspective.” in *Possible Worlds in Humanities, Arts and Sciences*, edited by Sture ALLÉN, pp. 93–123. Research in Text Theory n. 14. Berlin: de Gruyter. Proceedings of Nobel Symposium 65, doi:10.1515/9783110866858.93.
- PERRY, John R. 1989. “Possible Worlds and Subject Matter: Discussion of Partee (1989).” in *Possible Worlds in Humanities, Arts and Sciences*, edited by Sture ALLÉN, pp. 124–137. Research in Text Theory n. 14. Berlin: de Gruyter. Reprinted with a postscript in Perry (1993, 173–192) and in Perry (2000, 145–160), doi:10.1515/9783110866858.124.
- . 1993. *The Problem of the Essential Indexical and Other Essays*. New York: Oxford University Press, doi:10.1093/oso/9780195049992.001.0001.
- . 2000. *The Problem of the Essential Indexical and Other Essays*. Stanford, California: CSLI Publications. Enlarged edition of Perry (1993).
- SARTORIO, Carolina. 2005. “Causes as Difference-Makers.” *Philosophical Studies* 123(1/2): 71–96, doi:10.1007/s11098-004-5217-y.

- 717 SOBER, Elliott R. 1982. "Why Logically Equivalent Predicates May Pick Out Different  
718 Properties." *American Philosophical Quarterly* 19(2): 183–189.
- 719 STALNAKER, Robert C. 1984. *Inquiry*. Cambridge, Massachusetts: The MIT Press.
- 720 WALSH, Sean Drysdale. 2016. "Predicativity, the Russell-Myhill Paradox, and Church's  
721 Intensional Logic." *Journal of Philosophical Logic* 45(3): 277–326, doi:[10.1007/s1](https://doi.org/10.1007/s10992-015-9375-5)  
722 [0992-015-9375-5](https://doi.org/10.1007/s10992-015-9375-5).
- 723 YU, Andy Demfree. 2017. "A Modal Account of Propositions." *Dialectica* 71(4): 463–488,  
724 doi:[10.1111/1746-8361.12193](https://doi.org/10.1111/1746-8361.12193).

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